So you think you have all the data?

Causes and consequences of selection bias

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The promise of big data:

“Out with every theory of human behavior, from linguistics to sociology. Forget taxonomy, ontology, and psychology. Who knows why people do what they do? The point is they do it, and we can track and measure it with unprecedented fidelity. With enough data, **the numbers speak for themselves.**”

Chris Anderson *Wired* in an article called ‘*The end of theory: the data deluge makes scientific method obsolete*’

and endless similar by others
But things are not that simple

Big data carries risks

The risks associated with ‘small data’ and more

Today I will discuss just one of those risks
SELECTION BIAS
OUTLINE

Where I first met selection bias
The ubiquity of selection bias
Some drivers of selection bias
What to do about selection bias
Some more examples
Conclusion
WHERE I FIRST MET SELECTION BIAS:

1984 consultancy project for a UK consumer bank

The task: could I build an improved scorecard?
Available data: sample of people with known descriptors (application form) and with known (good/bad) outcome

The problem: the available data were not a random sample (or even a probability sample) from the population of future applicants:
e.g. Number of weeks since last CCJ
(from a different data set)

<table>
<thead>
<tr>
<th>Weeks</th>
<th>% G in whole pop</th>
<th>% G in design data</th>
<th>Ratio</th>
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<tr>
<td>1-26</td>
<td>22.7</td>
<td>44.6</td>
<td>1.964</td>
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<td>30.4</td>
<td>46.9</td>
<td>1.542</td>
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<tr>
<td>53-104</td>
<td>31.4</td>
<td>49.2</td>
<td>1.567</td>
</tr>
<tr>
<td>105-208</td>
<td>37.8</td>
<td>55.2</td>
<td>1.460</td>
</tr>
<tr>
<td>209-312</td>
<td>42.6</td>
<td>63.1</td>
<td>1.481</td>
</tr>
<tr>
<td>&gt; 312</td>
<td>55.6</td>
<td>69.2</td>
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</table>
SELECTION BIAS IS UBIQUITOUS:

Example 1: Potholes

- *Streetbump* smartphone app
- Detects potholes using accelerometer and emails location to local authority using GPS
- “Big data”, but no sophisticated computation or analytics
**SELECTION BIAS IS UBIQUITOUS:**

**Example 1: Potholes**

- *Streetbump* smartphone app
- Detects potholes using accelerometer and emails location to local authority using GPS
- “Big data”, but no sophisticated computation or analytics
- **But** lower income people less likely to have smartphones and cars, older people less likely to have smartphones, ...

→ streets in richer areas get fixed
Example 2: Hurricane Sandy

20 million tweets between 27 October and 1 November 2012

*But* a distorted impression of where problems are:
- most tweets came from Manhattan
- few from “more severely affected locations, such as Breezy Point, Coney Island and Rockaway”
- because of relative density of population/smartphones
- because power outages meant phones not recharged

→ distorted impression of where the damage occurred
Example 3: Publication bias

Relevant factors include:
- tendency not to submit negative results (file-drawer effect)
- positive results are more interesting to editors;
- anomalous results may be regarded as errors, and not submitted;

In an exploration of publication bias in the Cochrane database of systematic reviews:

“In the meta-analyses of efficacy, outcomes favoring treatment had on average a 27% ... higher probability to be included than other outcomes. In the meta-analyses of safety, results showing no evidence of adverse effects were on average 78% ... more likely to be included than results demonstrating that adverse effects existed.”

Kicinski et al 5015
**SOME DRIVERS OF SELECTION BIAS:**

1) *Natural mechanisms*

*Abraham Wald and the WWII bomber armour*

The bullet holes in returning bombers showed where they could be hit without bringing them down

A lesson for business schools? Look at the failures, not the successes

*Francis Bacon*

“when they showed him hanging in a temple a picture of those who had paid their vows as having escaped shipwreck, and would have him say whether he did not now acknowledge the power of the gods — ‘Aye,’ asked he again, ‘but where are they painted that were drowned after their vows?’ "
2) Non-response, refusals, and dropouts


3) **Self-selection**

(i) The magazine survey which asks the one question: *do you reply to magazine surveys?*

(ii) The *Literary Digest disastrous prediction* that Landon would beat Roosevelt in the 1936 presidential election

Standard explanation: the prediction was based on polling people with phones, who are more likely to be Republican

*But this is a myth*

In fact 10m people were polled, but only 2.3m replied

A self-selected sample, and in this election the anti-Roosevelt voters felt more strongly than the pro
(iii) *The Actuary* edition of July 2006 included an editorial which said ‘A couple of months ago I invited you - all 16,245 of you - to participate in our online survey concerning the sex of actuarial offspring. ... Well, I’m pleased to say that a number of you (13, in fact) replied to our poll.’

Particularly web-based surveys

- who replies?
- under-representation of some groups
- multiple responding
4) Feedback and asymmetric information

(i) The market for lemons

The buyer of a used car, with no further information on the vehicle in question, offers the average price of such vehicles.

The seller can keep the better quality ones and sell only the poor quality ones.
(ii) Crimemaps
But

People will not bother to report minor crime if they feel there’s no point

or for other reasons

“More than 5.2 million people have not reported crimes for fear of deterring home buyers or renters since the online crime map was launched in February 2011”

“A quarter (24 per cent) of people would not report a crime for fear it would harm their chances of selling or renting their property”

http://www.directline.com/media/archive-2011/news-11072011
WHAT TO DO ABOUT SELECTION BIAS:

1) *Construct and stick to sampling frame*

Or use “gold samples”

   Draw *some* cases from throughout the sample space

   Then standardise
2) *Registers*

e.g. in surveys of people

e.g. pre-registration in clinical trials

September 2004: *NEJM, Lancet, Annals of Internal Medicine, JAMA*: required drug research sponsored by pharmaceutical companies to be pre-registered in a public database as a precondition for publication
3) Detecting, e.g. publication bias

**Caliper tests**: ratio of reported results just above and just below the critical value associated with (e.g.) \( p = 0.05 \)

**Funnel plots** (and tests derived from them) are based on the law of small numbers

- large studies are likely to be published regardless of results
- small studies are likely to be published only if the results are “interesting”, i.e. significant
A relationship between sample size and effect size is suspicious. Hence the overabundance of plots in the bottom right of the funnel and the dearth in the left.
4) *Model the selection mechanism*

Heckman selection models (Nobel Prize)

Copas publication bias correction models

Rubin’s taxonomy of missing data mechanisms
SOME MORE EXAMPLES:
Example 1: Comparing scorecards

Scorecards need to be monitored
- are they still performing well (populations of applicants change; economic conditions change; competitive environment changes)
- new potential scorecard suppliers appear

Leading to the question:

Is scorecard C (challenger) better than scorecard I (incumbent)?

The data: accept applicants if $S_I > 0$

Which means that I and C are treated asymmetrically
Example:

Two classes, scores \((I,C)\)

- **Goods** distribution: bivariate normal means \((2,2), \rho=0.73, \sigma^2=1\)
- **Bads** distribution: bivariate normal means \((0,0), \rho=0.73, \sigma^2=1\)

**Incumbent and Challenger** have identical marginal distributions

\[ \Rightarrow \text{Incumbent and Challenger have identical performance in separating the goods from the bads} \]
But now suppose that applicants are accepted using the *Incumbent*
  i.e. truncate *Incumbent* at score 1

$\Rightarrow$ *Incumbent* distributions are *truncated normal*
$\Rightarrow$ *Challenger* distributions are *skew normal*

If the selection process is not included in the modelling, this means the separation of the marginal distributions is greater for the *Challenger* than for the *Incumbent*

An analysis ignoring the selection mechanism favours the *Challenger*
Example 2: Credit card fraud detection

Transaction stream terminated when incumbent detects a fraudulent transaction, not when the challenger does

→ data asymmetry

Standard fraud detection measures, ignoring the asymmetric data selection, favour the incumbent

But perhaps the challenger is quicker or cheaper ...
CONCLUSION:

When people say

*the numbers speak for themselves*
CONCLUSION:

When people say

*the numbers speak for themselves*

The real danger is that

*the numbers might be lying*
Expect selection distortion

Model selection distortion

Or risk mistaken conclusions
- loss of money
- risk to life
- ....
thank you!